

# Metaphor and Linguistic Creativity: Pragmatic Reasoning with Distributional Semantics

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This manuscript was compiled on June 1, 2019

1 **Humans create and interpret novel metaphors, like *Time is a thief* or**  
2 ***My lawyer is a shark*, with relative ease, incorporating world knowl-**  
3 **edge to determine which aspects of the predicate (*thief, shark*) are**  
4 **true of the subject (*time, my lawyer*). Here we present a computa-**  
5 **tional theory of metaphor, according to which metaphorical interpre-**  
6 **tations arise from joint, cooperative reasoning between a speaker**  
7 **and listener. We combine a Bayesian model of this reasoning pro-**  
8 **cess with empirically learned word embeddings which are used to**  
9 **provide an underlying representation of word meaning. This al-**  
10 **lows for open-domain interpretation of predicative and adjectival**  
11 **metaphors. We find a significant preference in human judgments**  
12 **for our model over a system which uses word embeddings without a**  
13 **explicit representation of inter-agent reasoning, providing evidence**  
14 **that reasoning about an informative and relevant speaker is key to**  
15 **understanding non-literal language.**

metaphor | informativity | Bayesian pragmatics | distributional semantics

1 Metaphor presents a compelling theoretical challenge for  
2 the understanding of meaning in natural language. On hearing  
3 (1) in a context where the subject, Jane, is known to be a  
4 journalist, a listener might infer that Jane is not literally a  
5 soldier, but rather that she shares certain attributes with  
6 soldiers (perhaps determination, endurance, or ruthlessness).

7 (1) Jane is a soldier

8 The *pragmatic* view of metaphor, proposed by Grice (1),  
9 takes the meaning conveyed by sentence (1) to be the result  
10 of joint, cooperative reasoning between a speaker and listener.  
11 That is, the speaker has some information about Jane, and  
12 wants to communicate some aspects of this information to  
13 the listener using the predicate *soldier*. The listener, in turn,  
14 jointly infers what Jane must be like and what aspects of Jane  
15 are relevant for the speaker.

16 **Interpreting figurative language** We build on a previous model  
17 of metaphor interpretation (2), developed as part of a proba-  
18 bilistic framework for pragmatic reasoning (3), which uses  
19 *projection functions* to determine the dimension of the world  
20 that the speaker cares about communicating. In this model, a  
21 listener jointly reasons about the state of the world (e.g. what  
22 Jane is like) and a projection function, corresponding to the  
23 aspect of the world the speaker cares to communicate (e.g.  
24 Jane's determination). This listener assumes an informative  
25 speaker - one whose choice of utterance maximizes the proba-  
26 bility of communicating the state of the world - but only up  
27 to a projection which dictates the relevant dimension of the  
28 world.

29 This can be used to give an account of predicative  
30 metaphors (those of the form *A is a B*) and adjective-noun

(AN) metaphors (like *fiery temper*). However, in order to  
generate predictions from the model, it is necessary to provide  
a semantics, specifying the literal meaning of each utterance  
(for example, that *soldier* literally describes an individual who  
serves in a military). Previous work has hand-constructed  
these literal interpretations, restricting the scalability of the  
models, and their applicability to previously unseen metaphors.

**Our contribution** We develop a model of pragmatic reasoning  
which uses empirically learned word-embeddings (4, 5) to repre-  
sent word meanings, obtaining a system capable of interpreting  
open-domain predicative and adjectival metaphors without the  
need for hand-specified semantics. This adaptation requires a  
generalization of projection functions to linear projections in  
a vector space, and a novel inference algorithm to calculate  
metaphor interpretations. Constructing this system permits  
what is to our knowledge the first open-domain evaluation  
of a Bayesian model of pragmatic reasoning. Evaluated on  
human judgments, our model significantly outperforms a base-  
line which uses a word embedding semantics without explicit  
pragmatic reasoning. This suggests that the information in  
word embeddings alone is not sufficient to capture the creativ-  
ity of metaphorical language, but that an explicit model of  
pragmatic reasoning is also key.

## 1. Overview of metaphor

Metaphor exists in many syntactic forms (6), and has been  
extensively studied in cognitive science (7–9), linguistics (10,  
11) and other disciplines (12, 13).

For present purposes, we focus on metaphors involving  
copular predicates (e.g. *Jane is a soldier*) and AN noun

### Significance Statement

Linguistic creativity — the ability to combine existing representa-  
tions to create new meanings — is a distinctive trait of human  
cognition. Metaphor provides a general vehicle for creative  
transfer and reuse of concepts. Here, we develop a system  
for open-domain interpretation of metaphor. Our system inte-  
grates world knowledge automatically induced from large text  
corpora, with reasoning about the social goals of the speaker.  
The approach provides a general architecture for composing  
semantic knowledge with social reasoning, providing insight  
into the origins of linguistic creativity.

R.C.G. and L.B. designed the model, planned the experiment, performed analyses, and wrote the  
manuscript. R.C.G. carried out the experiment.

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phrases (e.g. *fiery temper*). We refer to the predicated or modified noun (*Jane, temper*) as the *target* of the metaphor and the predicate or adjective (*soldier, fiery*) as the *source* (see (14) for the more general sense of these terms).

For a given metaphor, only certain properties of the target are described by the source, and which these are depend on both world knowledge and the semantics of the phrases. For instance, the use of the source *river* in (2) may convey that time flows in a single direction, whereas the same source in (3) may convey that the basement is flooded.

(2) Time is a river.

(3) The basement is a river.

While certain metaphors are conventional - comparing someone to a lion tends to connote bravery - examples like (2) and (3) suggest that the interpretation of a metaphor is dependent on semantic and world knowledge, factors which are naturally incorporated in a pragmatic model.

## 2. A Bayesian model of metaphor interpretation

The Rational Speech Acts framework (RSA) provides an elegant and practical way of formalizing pragmatic reasoning (3). In this framework, listeners and speakers are represented as conditional probability distributions. Speakers are represented as distributions over possible utterances given worlds, and listeners as distributions over possible worlds given utterances. The most basic version of RSA (3) is incapable of interpreting metaphors, due to the strict assumption that the speaker's utterances are literally true. To address this, Kao et al. (2) propose a model  $L_1^Q$ , shown in (6), which in turn is defined in terms of  $S_1$  (5) and  $L_0$  (4).

$$(4) L_0(w|u) \propto \llbracket u \rrbracket(w) \cdot P_L(w)$$

$$(5) S_1(u|w, q) \propto \sum_{w'} \delta_{q(w)=q(w')} \cdot L_0(w'|u)$$

$$(6) L_1^Q(w, q|u) \propto S_1(u|q, w) \cdot P_L(w) \cdot P_{L_Q}(q)$$

**The literal listener**  $L_0$  represents a model of a listener that, given an utterance  $u \in U$ , updates their belief about the world  $w \in W$  by filtering out all worlds that are semantically incompatible with  $u$ . The term  $\llbracket \cdot \rrbracket$  is a function  $U \rightarrow (W \rightarrow \{0, 1\})$ , representing the semantics of the language.  $P_L(w)$  is the prior probability of world  $w$ .

**Projections** Functions  $q \in Q$  formalize the notion of picking a particular *aspect* or *dimension* of  $w$ . Formally, they are functions  $W \rightarrow D$ , for some set  $D$ .

**The informative speaker**  $S_1$  has a state  $w$  they want to communicate to the listener  $L_0$ , and prefers utterances  $u$  which maximize the probability that  $L_0$  assigns to  $w$ , up to the dimension of  $w$  specified by  $q$ .  $\delta_{a=b}$  is an indicator function, and is equal to 1 if  $a = b$ , and equal to 0 otherwise. If  $q$  is the identity function, then  $S_1(u|w) \propto L_0(w|u)$ , and  $S_1$  is thus a model of a speaker who prefers to choose the most informative utterance available.

**The pragmatic listener** The full model,  $L_1^Q$ , hears an utterance  $u$ , and jointly infers values for  $w$  and  $q$  by reasoning about  $S_1$ . The key dynamic is that the listener may hear an utterance  $u$  and infer a pair  $(w, q)$  where  $u$  is semantically incompatible with  $w$  (i.e.  $\llbracket u \rrbracket(w) = 0$ ); this will occur when  $u$  conveys

effectively some feature of world  $w$  as determined by  $q$ .  $P_{L_Q}(q)$  is the prior probability of projection  $q$ .

$L_1^Q$  functions as a model of metaphor interpretation. For instance, using the metaphor in (7), the listener infers both a state  $w$  (representing what John is like) and a feature  $q$  (representing which aspects of John are relevant).

As an example in a hand-constructed setting, we could take John to be fully characterized by two features, whether he is vicious and whether he is aquatic, so that a state  $w$  is a value (true or false) for both of these predicates. The projections  $q \in Q$  are then the functions mapping a state to its value on viciousness ( $q_{vicious}$ ) or aquaticness ( $q_{aquatic}$ ) respectively. Further, we assume that *shark* is semantically compatible only with the state in which John is both vicious and aquatic.

(7) John is a shark.

On hearing (7), the prior belief that John is not literally an aquatic animal leads  $L_1^Q$  to conclude that the speaker cares about conveying the viciousness dimension (i.e. has projection  $q_{vicious}$ ), and that John is vicious. See (2) for quantitative examples.

Importantly,  $L_1^Q$  can do more than simply using prior knowledge to interpret literally false statements in a flexible way. It is also capable of reasoning about alternative utterances: for instance, suppose we add a third property, *quickness*, so that *shark* is compatible only with the state in which John is quick, aquatic and vicious, and also add a third utterance, *dolphin*, compatible only with John being quick, aquatic and *not* vicious.

In this second example, when  $L_1^Q$  hears *shark*, it infers that John is more likely vicious than quick. This is because a speaker who wanted to communicate that John is vicious would only be able to use the utterance *shark*, whereas a speaker who wanted to communicate that John is quick would be able to choose between either *shark* or *dolphin*. The utterance *shark* is therefore more likely to have been produced by the speaker trying to communicate John's viciousness.

$L_1^Q$  can model AN metaphors in a similar way. For a phrase like *John's fiery temper*, the listener infers the features of John's temper that would explain why the speaker described it with *fiery*.

## 3. Distributional Semantics

*Word embeddings*, or *distributional semantic models*, provide a representation of word meanings that can be learned from large corpora of language data. In these models, word meanings are mapped to points in a high-dimensional vector space, such that words with similar meanings are mapped to nearby points in the space. The embeddings can be obtained either by dimensionality reduction of a word co-occurrence matrix (5) estimated from a corpus, or by extracting the weights of a statistical model (4, 15, 16) trained on a separate task. In both cases, word embeddings provide a way to empirically obtain fine grained connotations of lexical items (4), and have been used effectively in a number of NLP tasks (17–19).

Metaphor is an obvious candidate for approaches that use distributional semantics: a wide variety of attempts have been made to leverage the information inherent in pre-trained word vectors for the detection, interpretation and paraphrase of metaphor (see (20) for an overview of proposed systems).

172 We hypothesize that, while the information in high quality  
 173 word embeddings captures important aspects of meaning, a  
 174 cognitively realistic model of metaphor interpretation should  
 175 also incorporate pragmatic reasoning, of the sort formalized  
 176 in the RSA framework. We now explain how the  $L_1^Q$  model  
 177 described above can be combined with a distributional model  
 178 of word meaning.

#### 179 4. Bayesian pragmatics with distributional semantics

180 We now introduce a *vector* interpretation of  $L_1^Q$ . Importantly,  
 181 this requires no modification to equations (4-6). The crucial  
 182 difference is that our state space  $W$  is now not just a set, but  
 183 a vector space, so that elements  $w \in W$  are vectors. A word  
 184 embedding maps words to vectors ( $E : U \rightarrow W$ ). For our  
 185 application of the model, we assume the set of utterances  $U$  is  
 186 a set of adjectives.

187 **The listener's prior** To define a prior distribution  $P_L$  over the  
 188 vector space  $W$ , we use a multivariate spherical Gaussian  
 189 distribution  $P_N$ , which can be parametrized by a vector  $\mu$   
 190 for the mean and a single scalar  $\sigma$  (the covariance matrix is  
 191 assumed to be  $\sigma^2 I$ ). We define the prior over projections  $P_{L^Q}$   
 192 to be uniform (the set of projections is discussed below).

$$193 (8) \quad P_L(w) = P_N(w | \mu = E(\text{target}), \sigma = \sigma_1)$$

194 We can view the prior  $P_L$  as representing uncertainty over  
 195 the position of the entity or concept that the target noun (e.g.  
 196 *man* in “The man is a shark”) represents. The goal of the  
 197 speaker is to convey a position in the space to the listener, and  
 198 the goal of the listener is to infer what this position is. In this  
 199 sense, the speaker and listener are playing a spatial reference  
 200 game (21), in an abstract word embedding space. Our vector  
 201 semantics bears comparison to the *conceptual space* semantics  
 202 of (22), as well as the proposal for metaphor comprehension  
 203 of (23).

204 The prior distribution places more probability mass on  
 205 points closer to its mean. By setting the mean of the prior as  
 206  $E(\text{target})$ , we encode the listener’s assumption that the mean-  
 207 ing the speaker wishes to communicate is in the neighborhood  
 208 of the source noun.  $\sigma_1$  is a hyperparameter which determines  
 209 the extent of the listener’s prior uncertainty.

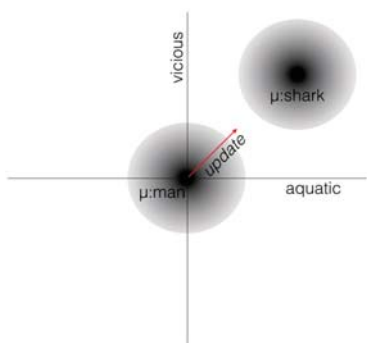


Fig. 1. Illustration of literal listener  $L_0$  given *The man is a shark*, with  $\overrightarrow{man} = (0,0)$  and  $\overrightarrow{shark} = (1,1)$ .  $L_0$ 's prior is centered at  $\overrightarrow{man}$ , and is updated towards *shark*.

210 **The semantics** Word embedding spaces allow us to compare  
 211 the similarity of words (e.g., a noun and an adjective) according  
 212 to different measures of distance in the space. However, they

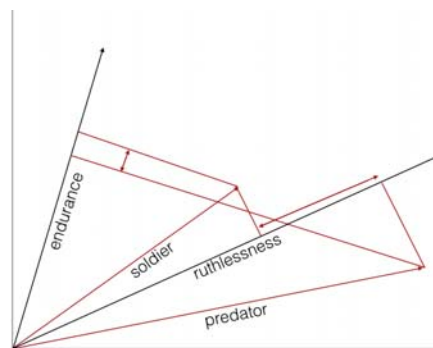


Fig. 2. In this hand-constructed 2D example, vectors for  $\overrightarrow{soldier}$  and  $\overrightarrow{predator}$  are projected onto subspaces given by  $\overrightarrow{endurance}$  and  $\overrightarrow{ruthlessness}$ . Soldiers have greater endurance than predators, while predators are more ruthless.

213 do not provide a means of categorically determining the com-  
 214 patibility of that adjective and noun, as previous pragmatic  
 215 models have required (described in Section 2). We observe,  
 216 however, that the definition of  $L_0$  in (4) only mathematically  
 217 requires that the semantics  $[\cdot]$  be a function  $U \rightarrow (W \rightarrow \mathbb{R})$ .  
 218 We can define such a function as follows, with  $\sigma_2$  as a hyper-  
 219 parameter:

$$220 (9) \quad [u](w) = P_N(w | \mu = E(\text{source}), \sigma = \sigma_2)$$

221 The value of  $[u](w)$  is a real number which decreases with  
 222 the Euclidean distance between  $u$  and  $w$ . The advantage of  
 223 defining the semantics in this way is that both the prior of  
 224  $L_0$ , shown in (8), and the likelihood, in (9), are Gaussian  
 225 distributions, which allows for a closed form solution of  $L_0$ ,  
 226 described in *Materials and Methods*.

227 **Projections** Finally, we need to supply a notion of a projection  
 228 function  $q$  that is defined on our vector space, and to specify  
 229 a set  $Q$  of such projections. For this, we use linear projections  
 230 along a vector (or hyperplane)  $v$  capturing the degree to  
 231 which each  $w$  extends along  $v$ , ignoring orthogonal dimensions.  
 232 Geometrically, this amounts to dropping a line from an input  
 233 vector  $w$  at a right angle onto  $v$ , as depicted in figure 2. These  
 234 projections exploit the linear structure of the embedding space  
 235 (5), which is documented more extensively in the setting of  
 236 word vectors than sentence vectors (15, 16), though see (24, 25)  
 237 for potential caveats.

238 In practice, we restrict ourselves to projections along a  
 239 vector, rather than a larger subspace. To obtain a set  $Q$  of  
 240 projections, we note that since word meanings are vectors in  
 241  $W$ , any word parametrizes a linear projection  $q$ . For instance,  
 242 we can think of the word *vicious* as defining a *viciousness*  
 243 projection, which measures how far other points in the space  
 244 fall along  $\overrightarrow{vicious}$ . We choose  $Q$  as a set of gradable adjectives,  
 245 so that the projection of a noun onto  $v$  amounts to asking: to  
 246 what extent does the noun have property  $v$ ? Figure 4 provides  
 247 a visualization of the  $L_1^Q$  posterior in a simple two-dimensional  
 248 case corresponding to the example discussed in section 2.

249 **Interpreting the output of  $L_1^Q$**  The *Materials and Methods* de-  
 250 scribes how to calculate the interpretation of a metaphor  
 251  $u$  given these assumptions. In particular, it shows how to  
 252 compute  $L_1^Q(w, q|u)$ , the joint distribution over states and  
 253 projections after hearing a metaphor  $u$ . Unlike points  $w \in W$ ,  
 254 projections  $q \in Q$  are readily interpretable, since they corre-  
 255 spond to adjectives, describing the aspect of the metaphorical

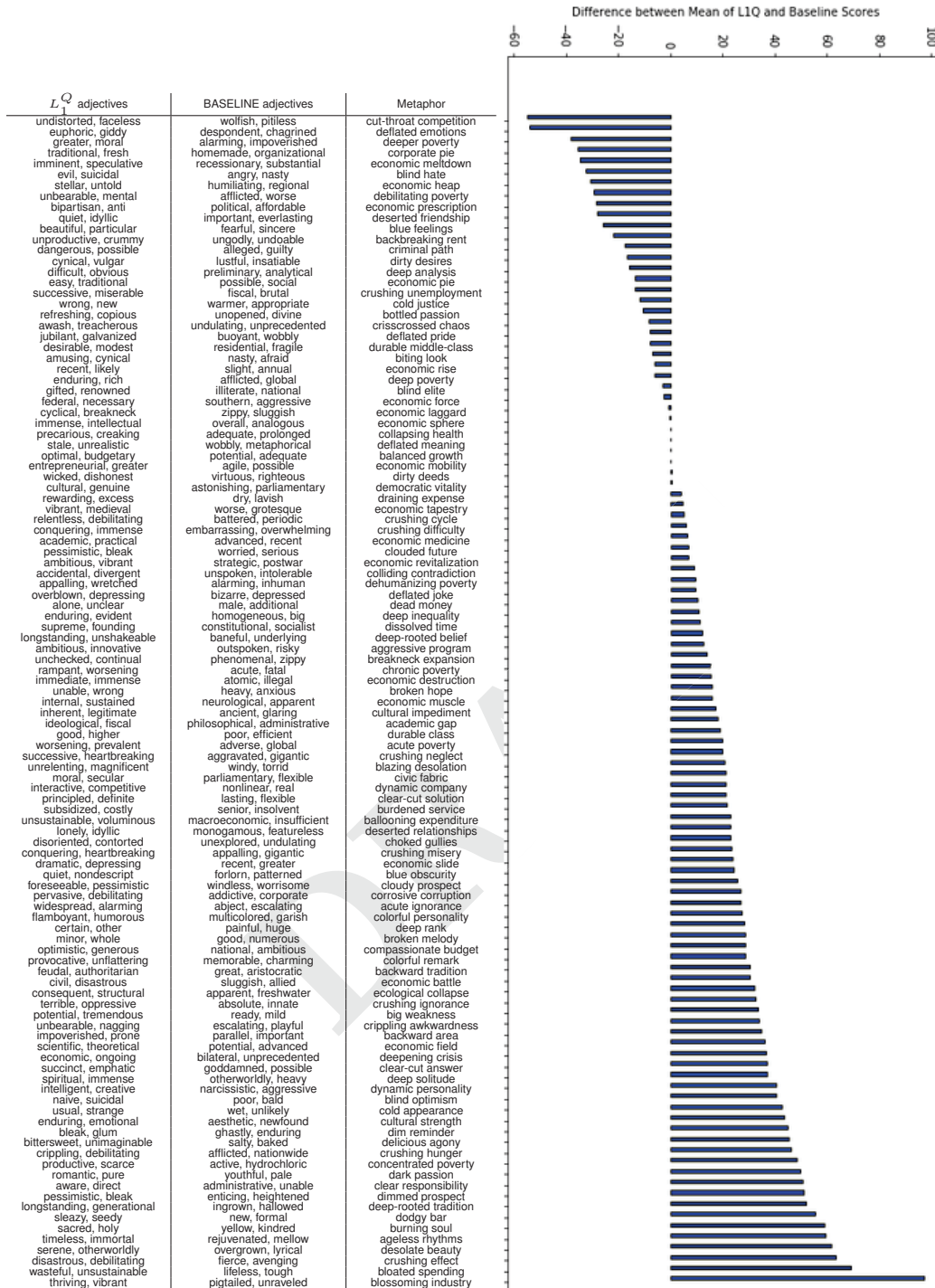
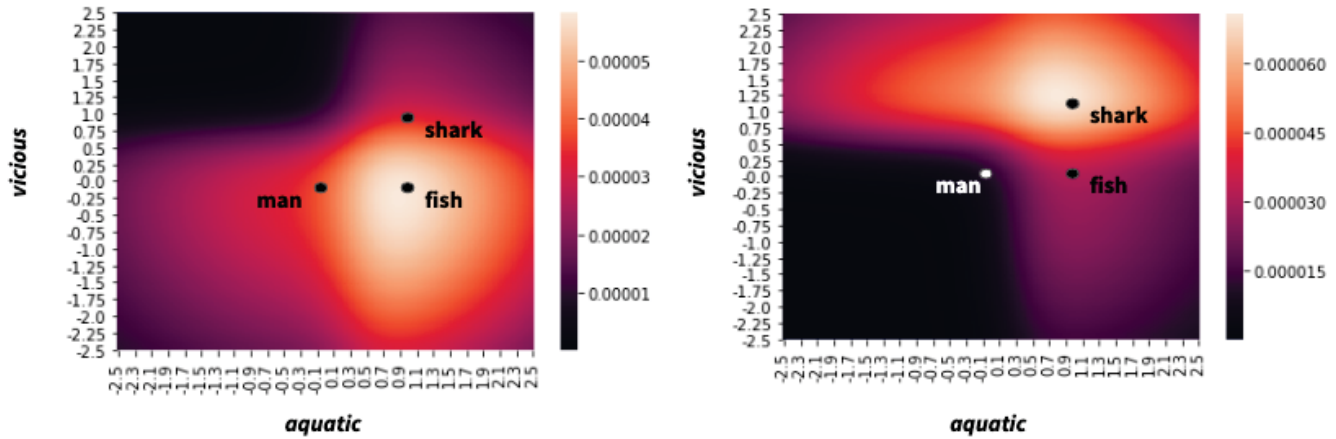


Fig. 3. The 109 metaphors used in the experiment, and baseline and  $L_1^Q$  interpretations. Bar positions indicate difference between judgments of  $L_1^Q$  and baseline proposals, averaged across participants and across both proposals of each model. Bars right of center indicate a preference for the pragmatic model, showing that for roughly 75% of the metaphors, the  $L_1^Q$  interpretation is preferred.



**Fig. 4.** Heatmaps visualizing the  $L_1^Q$  marginal posterior over states in a hand-constructed, two-dimensional case. The listener hears *The man is a fish* in the left panel, and *The man is a shark* in the right. The set of utterances  $U = \{man, shark, fish\}$ . For simplicity, the set of QUDs  $Q$  consists of orthogonal vectors, one along the x-axis (*aquatic*) and one along the y-axis (*vicious*). After hearing *fish*, the listener has lower uncertainty along the aquatic dimension, and higher uncertainty along the vicious dimension (left panel); after hearing *shark*, the situation is reversed (right panel).

256 adjective or predicate that is inferred to be relevant. For  
 257 this reason, we use the marginal posterior over  $Q$  to generate  
 258 predictions from the model. The top two  $L_1^Q$  marginal pos-  
 259 terior projections  $q$  for each metaphor, which we use in our  
 260 experiment, are shown in the leftmost column of Figure 3.

## 261 5. Experimental Evaluation

262 In order to evaluate whether pragmatic reasoning results in  
 263 metaphor interpretations that better capture human judg-  
 264 ments, we designed an experiment comparing  $L_1^Q$  interpre-  
 265 tations of metaphors to a baseline model which uses word  
 266 embeddings but no pragmatic reasoning.

267 **Experimental Design.** In the experiment, each participant was  
 268 shown a series of 12 adjectival metaphors, selected randomly  
 269 from a total of 109. For each metaphor, they were asked to  
 270 rate four candidate interpretations of the metaphor on a slider  
 271 bar. These four candidate interpretations consist of the best  
 272 and second best adjective generated by  $L_1^Q$ , and similarly for a  
 273 baseline model. The baseline model selects adjectives without  
 274 pragmatic reasoning, using a standard procedure from the  
 275 word embeddings literature (see *Materials and Methods*). An  
 276 example is shown in Figure 5.

277 **Analysis.** The results, shown in Figure 3, were analyzed using  
 278 mixed-effects models with random slopes and intercepts for  
 279 items and participants. Participants rated four interpretations  
 280 for each metaphor: the best and second-best interpretations,  
 281 as output by each of the target and baseline models. Partic-  
 282 ipants rated the target interpretations significantly higher  
 283 than the baseline interpretations ( $\beta=13.8$ ,  $t=5.3$ ,  $p < 10^{-7}$ )  
 284 in a combined analysis. The results were similar when the  
 285 best target interpretations were compared to the best base-  
 286 line interpretations ( $\beta=16.4$ ,  $t=4.8$ ,  $p < 10^{-5}$ ) and when the  
 287 second-best interpretations were compared ( $\beta=11.1$ ,  $t=3.2$ ,  
 288  $p < 0.005$ ).

## 289 6. Discussion

290 We have shown that it is possible to scale Bayesian pragmatic  
 291 reasoning to distributional semantics, and using this to obtain

a model of metaphor interpretation. Our evaluation, the first  
 open-domain evaluation of a Bayesian model of pragmatic  
 language interpretation, indicates that the principles of prag-  
 matic reasoning continue to operate at this scale, and are key  
 to obtaining human-like interpretations of metaphors. We  
 see this as an important step towards a cognitively accurate  
 and computationally tractable model of pragmatic language  
 interpretation and production in general.

## 300 Materials and Methods

302 **Model inference.** We employ a mix of analytic and approximate  
 303 methods to compute the  $L_1^Q$  distribution. We first present the  
 304 approach for computing  $L_0$  and  $S_1$  posteriors, which can be done  
 305 analytically, and then present the approximate inference algorithm  
 306 for  $L_1^Q$ . The implementation, written in TensorFlow, will be made  
 307 publicly available.

308  **$L_0$  Inference** The vector interpretation of  $L_0$  is illustrated in  
 309 Figure 1, where a ball, corresponding to the prior, is moved in  
 310 the direction of the point corresponding to the perceived utterance.  
 311 To calculate  $L_0$  analytically, we make use of Gaussian conjugacy.  
 312 When the prior  $P_L$  is defined as in Equation 8, and the semantic  
 313 interpretation is defined as in Equation 9, then conjugacy implies  
 314 that the listener posterior is given by:

$$(10) \quad L_0(w|u) = P_{\mathcal{N}}(w|\mu = \frac{\sigma_1^2 \sigma_2^2}{\sigma_1^2 + \sigma_2^2} (\frac{E(target)}{\sigma_1^2} + \frac{E(source)}{\sigma_2^2}), \sigma = \frac{\sigma_1^2 \sigma_2^2}{\sigma_1^2 + \sigma_2^2})$$

317  **$S_1$  Inference** The speaker is defined by Equation 5, which in the  
 318 continuous case can be rewritten as:

$$(11) \quad S_1(u|w, q) \propto \int_{w'} \delta_{q(w)=q(w')} \cdot L_0(w'|u)$$

320 Here  $q(w)$  is the projection of state  $w$  onto the subspace spanned by  
 321 projection vector  $q$ . This integral computes the marginal probability  
 322 of all states that are projected to the same location as  $w$  along  
 323  $q$ . From Equation 10,  $L_0(\cdot|u)$  is a normally distributed random  
 324 variable, and therefore the projection of this random variable onto a  
 325 linear subspace is also normally distributed, providing a closed-form  
 326 solution to  $S_1$ .

327  **$L_1^Q$  Inference** The  $L_1$  posterior is a joint distribution over one  
 328 continuous and one discrete random variable. Because of the linear  
 329 structure of the problem, we are able to devise a near-exact inference  
 330 algorithm for the marginal distribution over projections in  $Q$ , derived  
 331 as follows:

$$\begin{aligned}
L_1(q|u) &= \int_{\mathbb{R}^n} L_1(w, q|u) dw = \frac{1}{K} P_{L_Q}(q) \int_{\mathbb{R}^n} P_L(w) S_1(u|w, q) dw \\
&= \frac{1}{K} P_{L_Q}(q) \int_{\mathbb{R}^n} P_L(w_q, w_\perp) S_1(u|w_q, q) dw \\
&= \frac{1}{K} P_{L_Q}(q) \int_{D^\perp} P_L(w_\perp) dw_\perp \int_D P_L(w_q) S_1(u|w_q, q) dw_q \\
&= \frac{1}{K} P_{L_Q}(q) \int_D P_L(w_q) S_1(u|w_q, q) dw_q
\end{aligned}$$

Here  $K$  is a normalizing constant,  $w, q \in \mathbb{R}^n$ , and  $w_q$  is the projection of  $w$  onto the vector  $q$ .  $D$  is the subspace of  $\mathbb{R}^n$  spanned by the vector  $q$ , and  $D^\perp$  is the orthogonal complement of  $D$ . The vector  $w_\perp$  is the projection of vector  $w$  onto the subspace  $D^\perp$ . The final equation is a one-dimensional integral, and can be easily approximated. We use a Gaussian approximation, which easily generalizes to the setting of multi-dimensional projections. The constant  $K$  can be found from the constraint  $\sum_q L_1(q|u) = 1$ .

**Experiment.** The aim of our experiment is to determine whether pragmatic reasoning results in better interpretations of metaphors, according to human judgments. We compare against a lesioned model, with a distributional semantics that does not make use of pragmatic reasoning.

**Baseline model** Our baseline model is defined as follows: for a given metaphor of the form  $(a\ n)$ , we take the mean of the adjective word embedding  $E(a)$  and the noun word embedding  $E(n)$ . The two nearest adjectives  $q$  to this mean (measured by cosine distance) are the baseline interpretations for the metaphor. Taking the mean of word vectors is a standard technique for computing phrase and sentence meanings from constituent words (19, 26, 27), while cosine distance is commonly used to find words with the most similar meaning (5).

**$L_1^Q$  hyperparameters** We use the largest available (300 dimensional) GloVe vectors, as our word embedding  $E$ . For each Adjective-Noun metaphor  $(a\ n)$ , we specify  $U$  as a set of 101 alternative utterances, consisting of  $a$  and 100 of the nearest adjectives (by cosine distance) to  $n$ . These adjectives are chosen from the set of the 1425 adjectives with concreteness ranking  $> 3.0$  in the concreteness corpus of (28), to exclude abstract nouns. Similarly, we select a set  $Q$  of projections corresponding to the hundred closest adjectives to the mean of the subject and predicate (the method of adjective choice in the baseline model), and take  $P_{L_Q}$  to be a uniform distribution over  $Q$ .

By tuning on an independent validation set of metaphors, we choose  $\sigma_1 = \sigma_2 = 0.1$ ; all model parameters and features of the architecture were frozen prior to the experiment. Metaphor interpretations are generated by selecting the two projections with highest marginal posterior mass under  $L_1^Q$ . We choose two rather than one since the model tends to distribute most of its probability mass to at least two projections, intuitively reflecting the fact that there is usually more than one good interpretation of a metaphor.

**Experimental Methods** Tsvetkov et al. (29) provide a corpus of  $\sim 800$  AN metaphors, gathered by human annotators, from which we select the least frequent by bigram count (n-gram data from the Corpus of Contemporary American English (30)) to filter out conventionalized metaphors. Our full set of 109 metaphors is shown in figure 3. The data will be made available online. The experiment was run on Mechanical Turk, with 99 native English speakers. Participants who failed to follow instructions on a test item were excluded, leaving 60 participants (analyses remain significant with all participants included). Participants are shown a metaphor, as in figure 5 and asked to judge how relevant each proposed adjective (here, *debilitating*, *pervasive*, *corporate*, *addictive*) is to the metaphorical meaning of the AN phrase. In a test example, they are told to rate *intense* as relevant to *fiery temper* “because a fiery temper is an intense temper” but rate *warm* as irrelevant.

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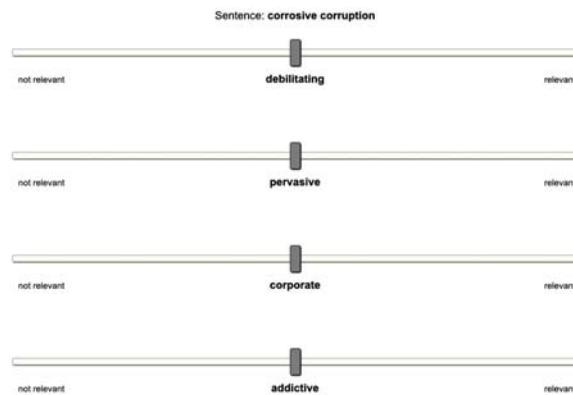


Fig. 5. An item in the experiment. Item order, and order of the 4 candidate adjectives are randomized.

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